SMA 6304
Factory Planning and Scheduling
Lecture 19: Material Requirements Planning

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MRP Overview

- *Primary source: Factory Physics* by Hopp and Spearman.
- *Basic idea:* Once the final due date for a product is known, and the time required for each production step is known, then intermediate due dates and material requirement times can be determined.
- *Original goal:* To determine when material for production is required.

Demand

- ... from outside the system is *independent* demand.
- ... for components or raw material is *dependent* demand.

Before MRP, buyers were not synchronized with producers.

MRP Overview

- Start at the due date for a finished product (or *end item*) (T_k).
- Determine the last operation, the time required for that operation (t_{k-1}), and the material required for that operation.
- The material may come from outside, or from earlier operations inside the factory.

MRP Overview

- Subtract the last operation time from the due date to determine when the last operation should start.

$$T_{k-1} = T_k - t_{k-1}$$

- The material required must be present at that time.
- Continue working backwards.
- *However, since more than one component may be needed at an operation, the planning algorithm must work its way backwards along each branch of a tree — the bill of materials.*

MRP Overview

Time

- In some MRP systems, time is divided into *time buckets* — days, weeks, or whatever is convenient.
- In others, time may be chosen as a continuous variable.

MRP Overview

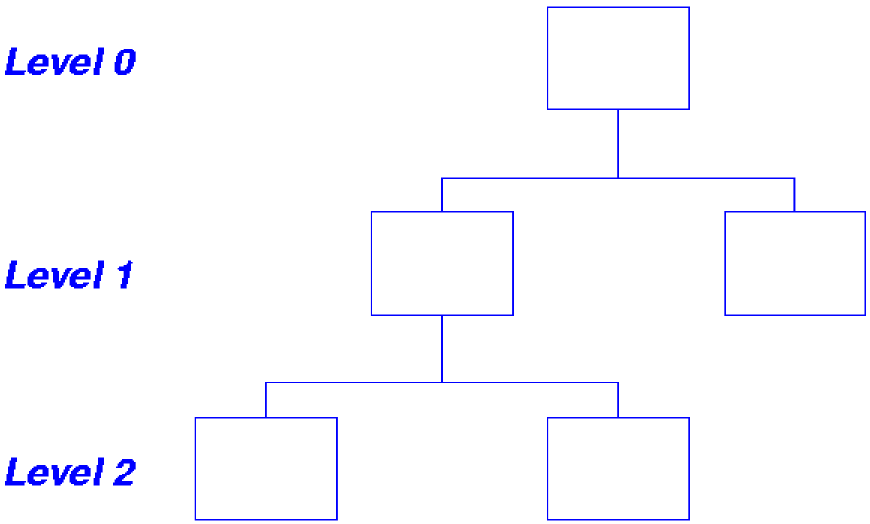
- What assumptions are being made here ...
  - ⋆ ... about predictability?
  - ⋆ ... about capacity?
- How realistic are those assumptions?
- Is it more flexible to use time buckets or continuous time?

MRP Overview

Jargon

- *Push system:* one in which material is loaded based on planning or forecasts, not on *current* demand.
  - ⋆ MRP is a push system.
- *Pull system:* one in which production occurs in response to the consumption of finished goods inventory by demand.
- *Which is better?*

Bill of Materials (BOM)



- Top level is end item.
- Items are given a *low-level code* corresponding to the lowest level they appear at, for any end item in the factory.

The BOM must be maintained as the product mix changes.

Master Production Schedule

- Information concerning independent demand.
- *Gross requirements:* What must be delivered in the future, and when.
- *On-hand inventory:* Finished good already available.
- *Net requirements:* (Gross requirements) – (On-hand inventory).

Master Production Schedule

Example

Netting

		Week							
		1	2	3	4	5	6	7	8
Gross requirements		15	20	50	10	30	30	30	30
Projected on-hand	30	15	-5						
Net requirements		0	5	50	10	30	30	30	30

- 15 of the initial 30 units of inventory are used to satisfy Week 1 demand.
- The remaining 15 units are 5 less than required to satisfy Week 2 demand.

Master Production Schedule

Example

Lot Sizing

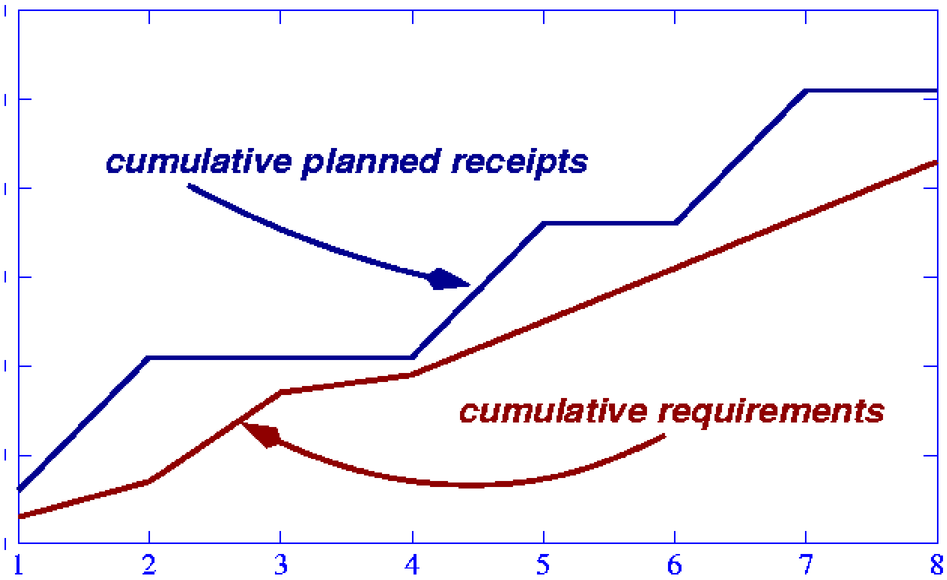
- Lot sizes are 75. The first arrival must occur in Week 2.
- 75 units last until Week 4, so plan arrival in Week 5.
- Similarly, deliveries needed in Weeks 5 and 7.

		Week							
		1	2	3	4	5	6	7	8
Gross requirements		15	20	50	10	30	30	30	30
Cumulative gross		15	35	85	95	125	155	185	215
Planned order receipts	30	0	75	0	0	75	0	75	0
Cumulative receipts		30	105	105	105	180	180	255	255

Master Production Schedule

Example

Cumulatives



Material requirements are determined by considering whether inventory would otherwise become negative.

Master Production Schedule

Example

Time Phasing

- Lead times are 1 week. Therefore, order *release* must occur one week before delivery is required.

		Week							
		1	2	3	4	5	6	7	8
Gross requirements		15	20	50	10	30	30	30	30
Cumulative gross		15	35	85	95	125	155	185	215
Planned receipts	30	0	75	0	0	75	0	75	0
Cumulative receipts		30	105	105	105	180	180	255	255
Planned release		75	0	0	75	0	75	0	0

- Now, do exactly the same thing for all the components required to produce the finished goods (level 1).
- Do it again for all the components of those components (level 2).
- Et cetera.

Data

- *Master Production Schedule* — demand – quantities and due dates
- *Item Master File* — for each part number: description, BOM, lot-sizing, planning lead times
- *Inventory Status* – finished goods, work-in-progress

Data

- *Planned order releases*
- *Change notices*
- *Exception reports* — discrepancies, consequences of unexpected events

Definitions

- Define
  - ⋆ D_t = Demands, or gross requirements for week t
  - ⋆ S_t = Quantity that will be completed in week t
  - ⋆ I_t = Projected finished inventory in week t
  - ⋆ N_t = Net requirements in week t

Netting

- Inventory dynamics: Starting with $t = 1$ (where $t = 0$ means *now*) and incrementing t by 1,

$$I_t = I_{t-1} - D_t, \text{ as long as } I_{t-1} - D_t \geq 0$$

$$I_t = I_{t-1} - D_t + S_t, \text{ if } I_{t-1} - D_t < 0$$

where S_t is minimal amount needed to make the inventory positive, which is consistent with lot-sizing requirements.

Netting

- Net requirements: Let t^* be the first time when $I_{t-1} - D_t < 0$. Then,

$$N_t = \begin{cases} 0 & \text{if} \quad t < t^* \\ I_{t-1} - D_t < 0 & \text{if} \quad t = t^* \\ D_t & \text{if} \quad t > t^* \end{cases}$$

- From net requirements, we calculate required production (scheduled receipts) $S_t, t > t^*$.
- S_t is adjusted for new orders or new forecasts.
- Then procedure is repeated for the next T^*.

Master Production Schedule

Netting

Example

		Week							
		1	2	3	4	5	6	7	8
Gross requirements		15	20	50	10	30	30	30	30
Projected on-hand	20	5	5	55	45	15	-15		
Adjusted scheduled receipts			20	100					
Net requirements		0	0	0	0	0	15	30	30

Master Production Schedule

Netting

Example

		Week						
		1	2	3	4	5	6	7
Gross requirements		15	20	50	10	30	30	30
Projected on-hand	20	5	5	55	45	15	-15	
Net requirements		0	0	0	0	0	15	30
Scheduled receipts*		10	10		100			
Adjusted scheduled receipts		0	20	100				

** original plan*

- The 10 units planned for week 1 were *deferred* to week 2.
- The 100 units planned for week 4 were *expedited* to week 3.

Possible rules:

- *Lot-for-lot:* produce in a period the net requirements for that period. *Maximum* setups.
- *Fixed order period:* produce in a period the net requirements for P periods.
- *Fixed order quantity:* always produce the same quantity, whenever anything is produced. EOQ formula can be used to determine lot size.

Which satisfy the Wagner-Whitin property?

BOM Explosion

- After scheduling production for all the top level (Level 0) items, do the same for Level 1 items.
- *The planned order releases for Level 0 are the gross requirements for Level 1.*
- Do the same for Level 2, 3, etc.

Reality

- MRP is deterministic but reality is not. Therefore, the system needs *safety stock* and *safety lead times* .
- Safety stock protects against quantity uncertainties.
  - ★ You don't know how much you will make, so plan to make a little extra.
- Safety lead time protects against timing uncertainties.
  - ★ You don't know exactly when you will make it, so plan to make it a little early.

Safety Stock

- Instead of having a minimal planned inventory of zero, the (positive) safety stock is the planned minimal inventory level.
- Whenever the actual minimal inventory differs from the safety stock, adjust planned order releases accordingly.

Safety Lead Time

- Add some extra time to the planned lead time.

- *Yield* = expected fraction of parts started that are successfully produced.
- Actual yield is random.
- If you need to end up with N items, and the yield is y, start with N/y.
- However, the actual production may differ from N, so safety stock is needed.

Reality

- Capacity is actually finite.
- Planned lead times tend to be long (to compensate for variability).
  - ★ Also, workers *should* start work on a job as soon as it is released, and relax later (usually possible because of safety lead time). Often, however, they relax first, so if a disruption occurs, the job is late.

- *Nervousness* — drastic changes in schedules due to small deviations from plans — *(chaos?)*
- Nervousness results when a deterministic calculation is applied to a random system, and local perturbations lead to global changes.

Reality

Other problems

Nervousness

- Possible consequences:
  - ⋆ Drastic changes in plans for the near future, which will confuse workers;
  - ⋆ Excessive setups, consuming excess expense or capacity.
- *Solution:* Freeze the early part of the schedule (ie, the near future). Do not change the schedule even if there is a change in requirements; or do not accept changes in requirements.
  - ⋆ *But:* What price is paid for freezing?

Reality

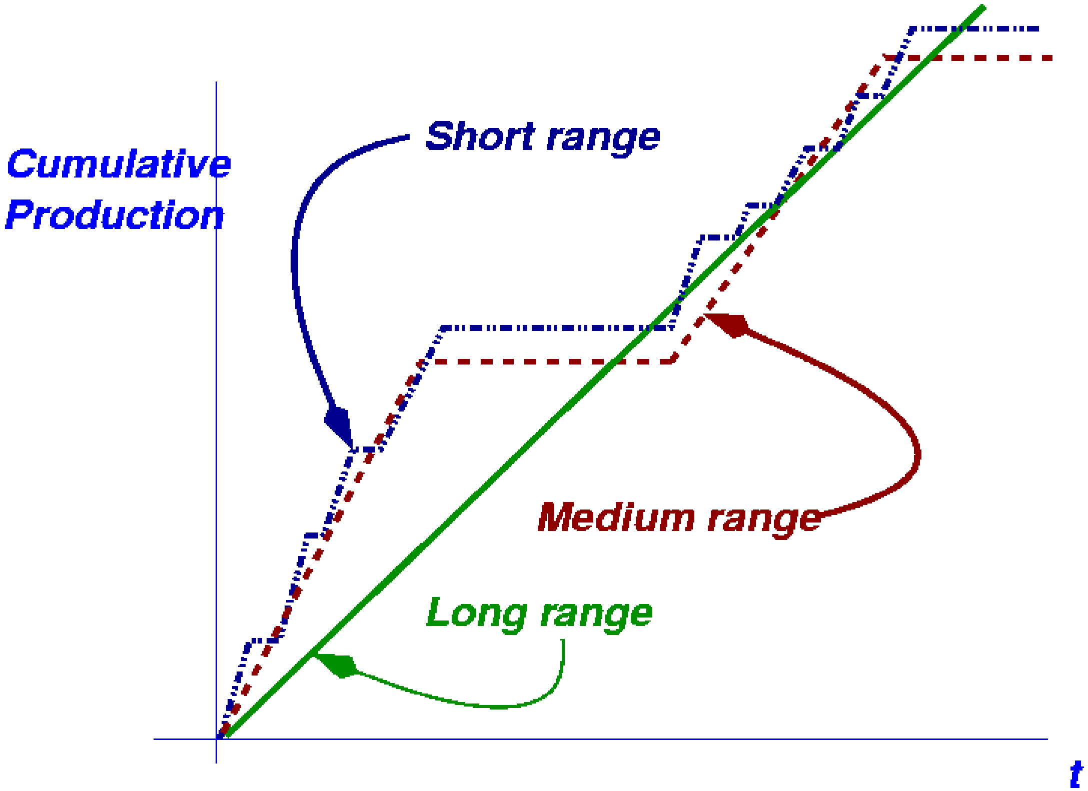
Fundamental problem

- *MRP is a solution to a problem whose formulation is based on an unrealistic model,* one which is
  - ⋆ deterministic
  - ⋆ infinite capacity
- As a result,
  - ⋆ it frequently produces non-optimal or infeasible schedules, and
  - ⋆ it requires constant manual intervention to compensate for poor schedules.
- *On top of that, nervousness amplifies inevitable variability.*

MRP II

- Manufacturing Resources Planning
  - ★ MRP, and correction of some its problems,
  - ★ demand management,
  - ★ forecasting,
  - ★ capacity planning,
  - ★ master production scheduling,
  - ★ rough-cut capacity planning,
  - ★ capacity requirements planning (CRP),
  - ★ dispatching,
  - ★ input-output control.

MRP II Hierarchy



Long-Range Planning

- Range: six months to five years.
- Recalculation frequency: 1/month to 1/year.
- Detail: part family.
- Forecasting
- Resource planning — build a new plant?
- Aggregate planning — determines rough estimates of production, staffing, etc.

MRP II Hierarchy

- Demand management — converts long range forecast and actual orders into detailed forecast.
- Master production scheduling
- Rough-cut capacity planning — capacity check for feasibility.
- CRP — better than rough cut, but still not perfect. Based on infinite capacity assumption.

MRP II Hierarchy

Short-Term Control

- Shop Floor Control
  - ★ Job dispatching — which job to run next?
  - ★ Input-output control — release
  - ★ often based on simple rules